Equity in the Time Series, Part 1

15.433 Financial Markets

September 28, 2017

This Version: September 26, 2017
Outline

- Predicting the Market.
- Market Efficiency.
Predicting the Market

- From quant investing: the alpha of a quant strategy comes from a certain ability to predict the future. But when it comes to the market risk, the approach is to avoid it by taking long/short positions.

- Yet, the market risk remains the most important and pervasive.

- So what do we know about predicting the aggregate stock market?
  - How good are investors at predicting the market?
  - How do professional investors view market timing?
  - Empirically, the dividend/price ratio is found to be a good predictor. How much of the future market returns can it predict?
Realized vs. Expected in an i.i.d. Model

- $R_t$: annual realized returns (%)
- $\mu$: annual expected returns (%)

Some Pick the Stock, Others Choose the Moment

BusinessWeek, February 19, 2007
Views on Market Timing

Excerpts from “Pioneering Portfolio Management” by David Swensen


- Careful investors consciously construct portfolios to reflect the expected contribution of each portfolio management tool.

- Market timing, according to Charles Ellis, represents a losing strategy: “There is no evidence of any large institutions having anything like consistent ability to get in when the market is low and get out when the market is high. Attempts to switch between stocks and bonds, or between stocks and cash, in anticipation of market moves have been unsuccessful much more often than they have been successful.”

- “Serious investors avoid timing markets.”
How Good are Professional Investors at Predicting the Market?

**TABLE 5-3**

Investor Confidence and Dow Price Returns, Sentiment = Bull/(Bull + Bear)

BULL and BEAR from Investors Intelligence Inc., New Rochelle, NY

<table>
<thead>
<tr>
<th>Sentiment</th>
<th>Frequency</th>
<th>Three Month</th>
<th>Six Month</th>
<th>Nine Month</th>
<th>Twelve Month</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.2 - 0.3</td>
<td>1.55%</td>
<td>18.52%</td>
<td>15.40%</td>
<td>22.79%</td>
<td>20.74%</td>
</tr>
<tr>
<td>0.3 - 0.4</td>
<td>11.30%</td>
<td>12.23%</td>
<td>13.87%</td>
<td>16.54%</td>
<td>15.81%</td>
</tr>
<tr>
<td>0.4 - 0.5</td>
<td>19.35%</td>
<td>16.85%</td>
<td>13.63%</td>
<td>12.07%</td>
<td>12.73%</td>
</tr>
<tr>
<td>0.5 - 0.6</td>
<td>27.90%</td>
<td>15.16%</td>
<td>14.06%</td>
<td>10.44%</td>
<td>8.82%</td>
</tr>
<tr>
<td>0.6 - 0.7</td>
<td>19.14%</td>
<td>14.03%</td>
<td>8.79%</td>
<td>8.71%</td>
<td>7.27%</td>
</tr>
<tr>
<td>0.7 - 0.8</td>
<td>14.76%</td>
<td>11.21%</td>
<td>7.24%</td>
<td>7.38%</td>
<td>7.01%</td>
</tr>
<tr>
<td>0.8 - 0.9</td>
<td>5.23%</td>
<td>-0.39%</td>
<td>0.23%</td>
<td>-3.32%</td>
<td>-1.79%</td>
</tr>
<tr>
<td>0.9 - 1.0</td>
<td>0.78%</td>
<td>0.35%</td>
<td>-3.87%</td>
<td>-9.17%</td>
<td>-10.18%</td>
</tr>
<tr>
<td>Overall</td>
<td>100.00%</td>
<td>13.48%</td>
<td>11.11%</td>
<td>9.99%</td>
<td>9.31%</td>
</tr>
</tbody>
</table>

Source: “Stocks for the Long Run” by Jeremy Siegel
Investor Expectations and Past Stock Returns

Investor Expectations and Equity Mutual Fund Flows

Running a Predictive Regression:

- Let $I_t$ be a candidate predictor, observable at time $t$:

$$R_{t+1} = a + b I_t + \epsilon_{t+1},$$

where $\epsilon_{t+1}$ is the *unpredictable* component of the stock return.

- If $b$ is statistically significant, then we have a potentially useful predictor.

- The best way to gauge the usefulness of a predictor is through the R-squared of the regression:

$$\text{R-squared} = \frac{\text{var}(b I_t)}{\text{var}(R_{t+1})}; \quad 1-\text{R-squared} = \frac{\text{var}(\epsilon_{t+1})}{\text{var}(R_{t+1})},$$

- Much effort has been spent on finding good predictors. Let’s take a look at some of them.
Can Past Returns Predict Future Returns?

\[ R_{t+1} = \alpha + \rho R_t + \epsilon_{t+1} \]

<table>
<thead>
<tr>
<th></th>
<th>rho (%)</th>
<th>t-stat</th>
<th>R-sqr (%)</th>
<th>sample period</th>
</tr>
</thead>
<tbody>
<tr>
<td>S&amp;P 500</td>
<td>11.3</td>
<td>2.28</td>
<td>1.27</td>
<td>1926-1960</td>
</tr>
<tr>
<td>CRSP Value Weight</td>
<td>12.1</td>
<td>2.46</td>
<td>1.47</td>
<td>1926-1960</td>
</tr>
<tr>
<td>CRSP Equal Weight</td>
<td>15.7</td>
<td>3.20</td>
<td>2.46</td>
<td>1926-1960</td>
</tr>
<tr>
<td>S&amp;P 500</td>
<td>3.9</td>
<td>1.01</td>
<td>0.15</td>
<td>1960-2015</td>
</tr>
<tr>
<td>CRSP Value Weight</td>
<td>3.9</td>
<td>1.01</td>
<td>0.15</td>
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</tr>
</tbody>
</table>

- Rho (\(\rho\)) measures the *auto-correlation* in the monthly stock returns.
- In Econometrics, this model is called AR(1), with AR for auto-regressive.
- The average rho for individual stocks is *negative* but insignificant.
Predictive Returns at Daily Frequency

\[ R_{t+1} = a + \rho R_t + \epsilon_{t+1} \]

<table>
<thead>
<tr>
<th></th>
<th>rho (%)</th>
<th>t-stat</th>
<th>R-sqr (%)</th>
<th>sample period</th>
</tr>
</thead>
<tbody>
<tr>
<td>S&amp;P 500</td>
<td>2.0</td>
<td>2.28</td>
<td>0.04</td>
<td>1962-2015</td>
</tr>
<tr>
<td>S&amp;P 500</td>
<td>-3.3</td>
<td>-3.02</td>
<td>0.11</td>
<td>1982-2015</td>
</tr>
<tr>
<td>S&amp;P 500</td>
<td>-7.7</td>
<td>-4.93</td>
<td>0.60</td>
<td>2000-2015</td>
</tr>
<tr>
<td>Yen/Dollar</td>
<td>0.5</td>
<td>0.35</td>
<td>0.0022</td>
<td>1995-2016</td>
</tr>
<tr>
<td>Yen/Dollar</td>
<td>0.3</td>
<td>0.30</td>
<td>0.0010</td>
<td>1980-2016</td>
</tr>
<tr>
<td>Yen/Dollar</td>
<td>0.3</td>
<td>0.28</td>
<td>0.0007</td>
<td>1970-2016</td>
</tr>
</tbody>
</table>
Day t-1: buy 1 USD of Yen at $Y_{t-1}$

Day t: sell this amount of Yen at $Y_t$

\[ R_t = \frac{Y_{t-1}}{Y_t} - 1 \]

\[ R_t = \log(Y_{t-1}) - \log(Y_t) \]

Since 1995:

- mean=-5bps
- std=11.09%

*both annualized using 261 days per year*
Time-Varying Expected Returns

- Only in an i.i.d. world does predictability mean market inefficiency.
- Otherwise, having a predictive component in market returns does not necessarily mean that markets are inefficient.
- The predictive component could be interpreted as time-varying expected returns:

  \[ \mu_t = E_t(R_{t+1}) = a + b I_t \]

- For example, time-varying business conditions or time-varying risk appetite could both be a cause for time-varying expected returns.
- Over longer horizons (e.g., business cycles), there is a closer connection between market returns and macroeconomic conditions.
NBER Dated Recessions (shaded areas)

Annual Stock Returns (in Percent) from 1927 through 2014
Predictors that are related to business conditions

- Default Spreads: *differences in yields between defaultable bonds and treasury bonds with similar maturities*. When the business condition is bad, the systematic default risk increases, widening the default spread.

- Term Premiums: *differences in yields between long- and short-term treasury bonds*. This is a forward-looking variable predictive of future inflation, and is found to be important in forecasting real economic activity.

- Financial Ratios: *dividend-price ratio*. Variables that are important in fundamental valuation. Could be proxies for systematic risks that are higher when times are poor, and lower when times are good.
Stock Return and Dividend-Price Ratio
Use Dividend-Price Ratio to Predict Stock Returns

\[ R_{t+1} = a + b \left( \frac{D}{P} \right)_t + \epsilon_{t+1} \]

- \( R_t \): annual stock return realized in year \( t \).
- \( (D/P)_t \): dividend-price ratio realized in year \( t \).

<table>
<thead>
<tr>
<th>1927-2008</th>
<th>a</th>
<th>b</th>
</tr>
</thead>
<tbody>
<tr>
<td>estimate</td>
<td>-0.02</td>
<td>3.22</td>
</tr>
<tr>
<td>standard error</td>
<td>0.06</td>
<td>1.34</td>
</tr>
<tr>
<td>t-stat</td>
<td>-0.36</td>
<td>2.40</td>
</tr>
</tbody>
</table>

- The R-squared of the regression: 6.63%.
- The sample standard deviation of \( D/P \) is 1.68%.
Realized vs. Expected Returns

- Realized Stock Return
- Predicted Stock Returns
- i.i.d. Model
Market Efficiency

- Follow the information:
  - Orange juice and the weather in Orlando, Florida.
  - Speed of price discovery and the value of millisecond.

- The force of arbitrage and traditional convergence trades:
  - Equity: index futures and the cash market.
  - Fixed Income: old and new bonds on the Treasury yield curve.
  - FX: covered interest-rate parity.

- Limits to arbitrage.
  - Limited balance sheet capacity and access to funding.
  - Uncertainty: Bubble or not?